

$y - b = m(x - a)$  is the eq<sup>n</sup> of the  
line with slope  $(m) = 44$   
through point  $(a, b)$

$$y - 1400 = 44(x - 0)$$

$(0, 1400)$

$$y = 44x + 1400$$

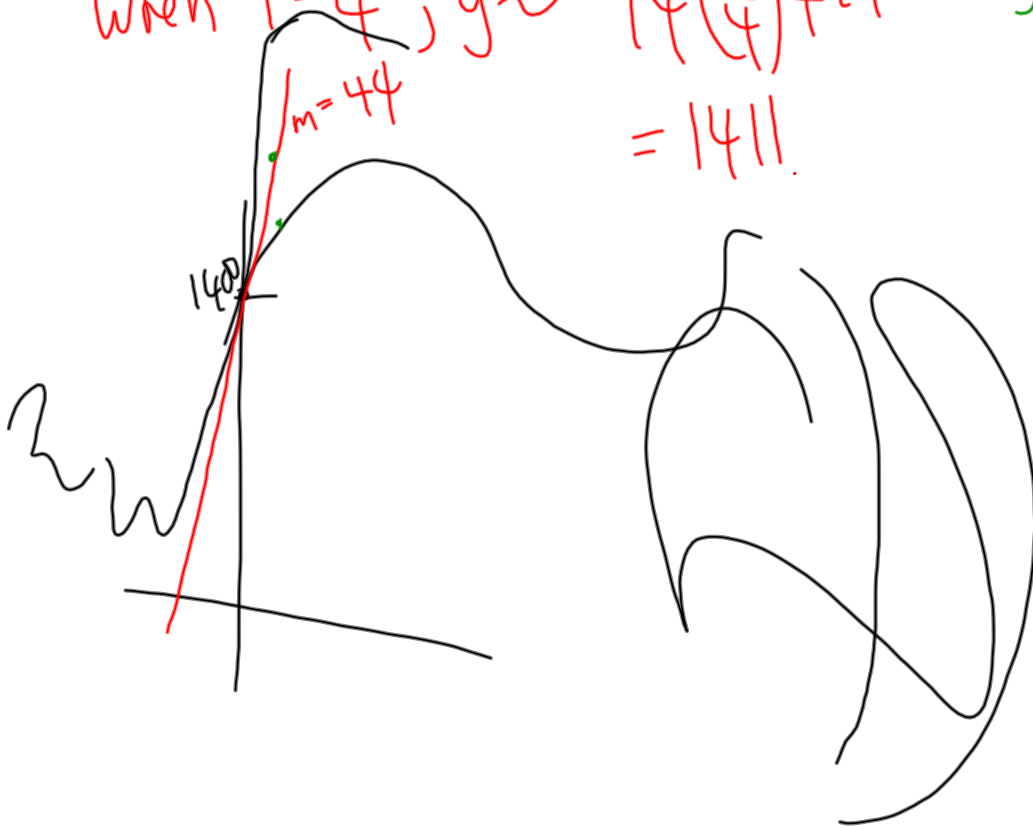
$$y = mx + B$$

$$b = ma + B$$

$$(b - ma) = B$$

$$y = mx + (b - ma)$$

when  $t = \frac{1}{4}$ ,  $y \approx 44\left(\frac{1}{4}\right) + 1400$   
 $= 1411$



$$\frac{dW}{dt} = \frac{1}{25}(W-300)$$

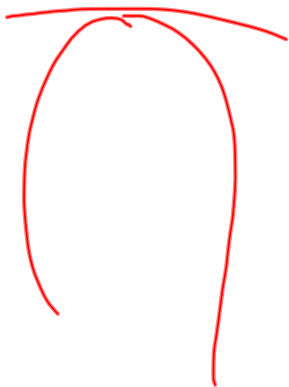
b) find  $\frac{d^2W}{dt^2}$  in terms of  $W$

$$\frac{d^2W}{dt^2} = \frac{1}{25} \left( \frac{dW}{dt} \right)$$

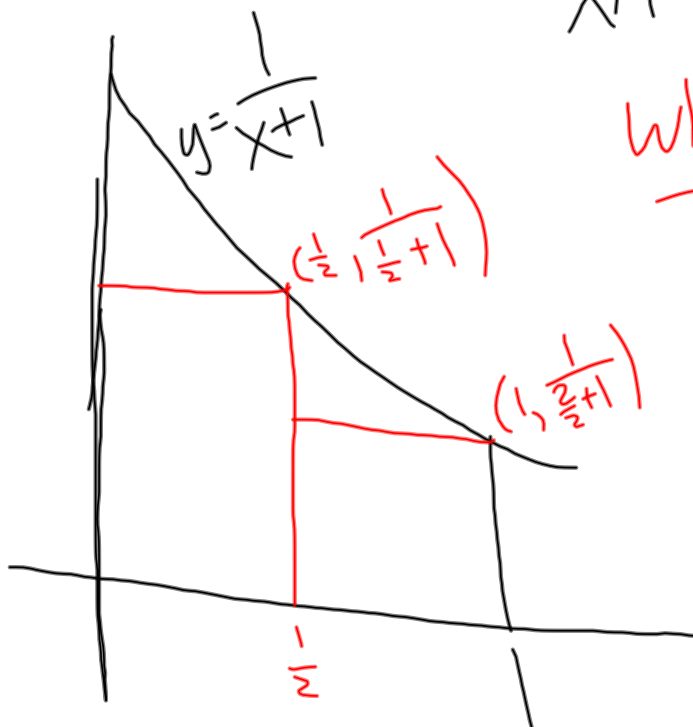
$$\frac{d^2W}{dt^2} = \frac{1}{25} \left( \frac{1}{25}(W-300) \right)$$



How do I use SECOND derivative to determine if tangent line is ABOVE or BELOW the curve?



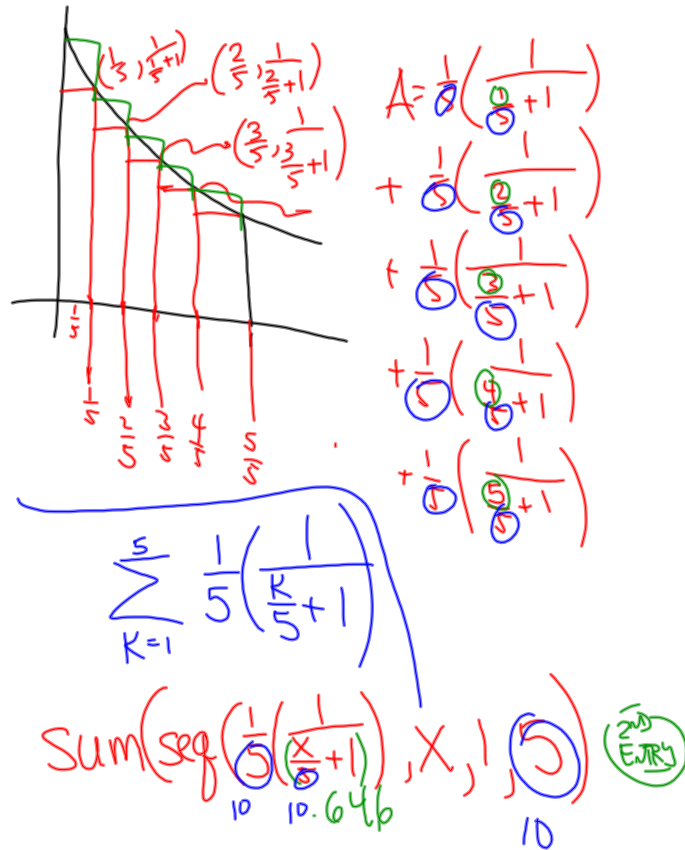
6.1) 2       $f(x) = \frac{1}{x+1}; \quad [0, 1]$



when  $n=2$

$$A = \left(\frac{1}{2}\right)\left(\frac{1}{\frac{1}{2}+1}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{\frac{1}{2}+1}\right)$$

6.1/2  $n=5$



$n=10$   
 $.669$   
 $n=5$ , but height of rectangle =  $f(\text{left side})$

$$\sum_{k=0}^4 \frac{1}{5} \left( \frac{1}{\frac{k}{5} + 1} \right)$$

$$\text{Sum}(\text{seq}(\frac{1}{5}(\frac{1}{\frac{x}{5} + 1}), X, 0, 4)$$

$\{ \frac{1}{1}, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \frac{1}{5} \}$   
 $\text{SEQ}(\frac{1}{x}, X, 1, 5)$   
 create a sequence where each term looks like  
 and the variable is going to change by +1, starting at  
 and finishing when I wind up

$$\sin x \quad [0, \pi]$$



$$\sum_{k=1}^{10} \frac{\pi}{10} \left( \sin\left(\frac{k\pi}{10}\right) \right)$$

$$\text{Seq}\left( \quad, K, 1, 10 \right)$$

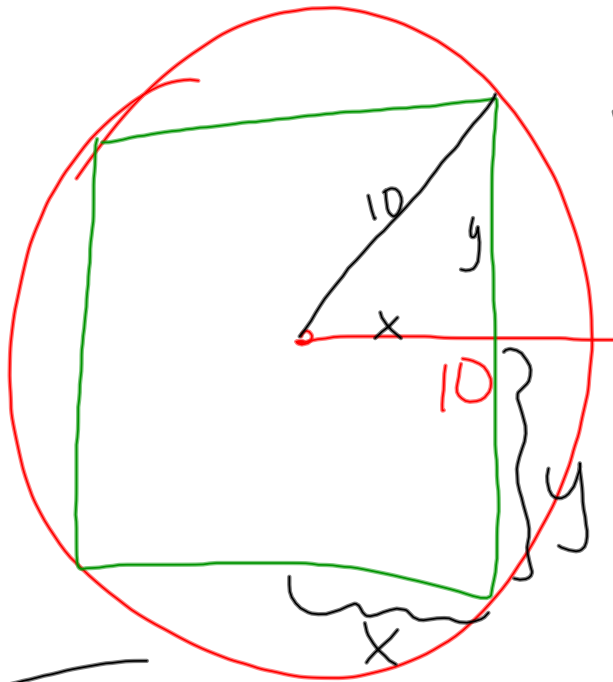
✓

Bye.

5.6/  
~~9~~

$$A = (2x)(2y) \\ = 4xy$$

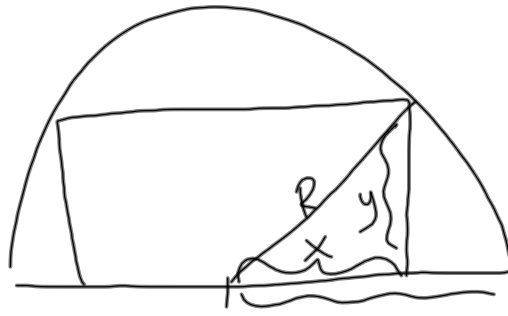
$$= 4x\sqrt{100-x^2}$$



$$x^2 + y^2 = 10^2$$

$$y = \sqrt{100 - x^2}$$

5.6/10



$$A = (2x)y$$
$$= 2xy$$

$$x^2 + y^2 = R^2$$

$$A = 2x\sqrt{R^2 - x^2}$$

$$y^2 = R^2 - x^2$$

$$y = \sqrt{R^2 - x^2}$$

$$\frac{dA}{dx} = 2\sqrt{R^2 - x^2} - \frac{4x^2}{\sqrt{R^2 - x^2}}$$

$$\frac{dA}{dx} = \frac{2\sqrt{R^2 - x^2}\sqrt{R^2 - x^2}}{\sqrt{R^2 - x^2}} - \frac{4x^2}{\sqrt{R^2 - x^2}}$$

$$\frac{dA}{dx} = \frac{2(R^2 - x^2) - 4x^2}{\sqrt{R^2 - x^2}}$$

$= 0$  when

$2R^2 - 2x^2 - 4x^2 = 0$

$2R^2 - 6x^2 = 0$

$x = \pm \sqrt{\frac{1}{3}} R$

und?  
 $x = R$

$$\frac{dW}{dt} = \frac{1}{25}(W - 300)$$

$$m = \frac{dW}{dt} \text{ at } \begin{pmatrix} t=0 \\ W=1400 \end{pmatrix} = \frac{1}{25}(1400 - 300) \\ = \frac{1100}{25} = 44$$

$$P_t = (0, 1400)$$

$$\begin{array}{l} \text{tangent} \\ \text{line} \end{array} \left\{ \begin{array}{l} y - 1400 = 44(x - 0) \\ y = 44x + 1400 \end{array} \right.$$

Use when  $t = \frac{1}{4}$

$$y = 44\left(\frac{1}{4}\right) + 1400 \\ = 11 + 1400 = 1411 \text{ tons}$$



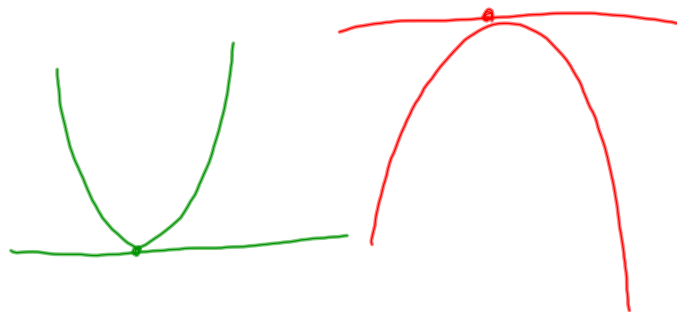
$$b) \quad \frac{dW}{dt} = \frac{1}{25}(W-300)$$

$$\frac{dW}{dt} = \frac{1}{25}W - 12$$

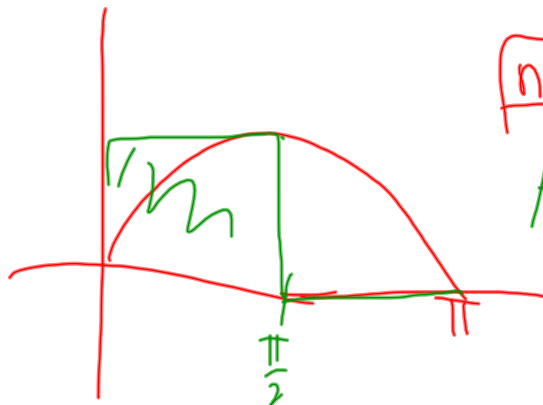
$$\frac{d^2W}{dt^2} = \frac{1}{25} \left( \frac{dW}{dt} \right)$$

$$\frac{d^2W}{dt^2} = \frac{1}{25} \left( \frac{1}{25}(W-300) \right)$$

How does the second derivative  
tell me if tangent line is ABOVE  
or BELOW the curve?

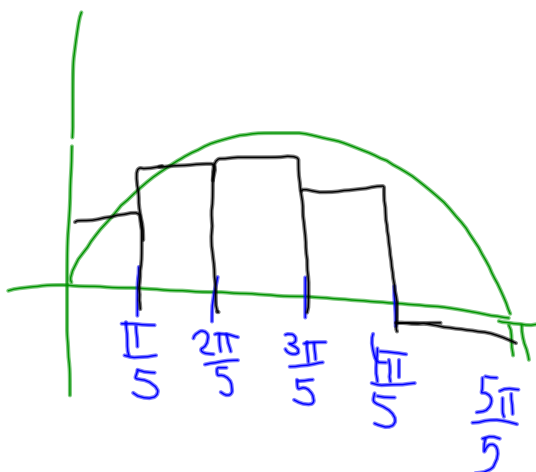


6.1/3)  $f(x) = \sin x \quad [0, \pi]$



$n=2$

$$A = \left(\frac{\pi}{2}\right) \sin \frac{\pi}{2} + \left(\frac{\pi}{2}\right) \sin \frac{2\pi}{2} = \frac{\pi}{2}$$



$$A = \left(\frac{\pi}{5}\right) \left(\sin \frac{\pi}{5}\right)$$

$$+ \left(\frac{\pi}{5}\right) \left(\sin \frac{2\pi}{5}\right)$$

$$+ \left(\frac{\pi}{5}\right) \left(\sin \frac{3\pi}{5}\right)$$

$$+ \left(\frac{\pi}{5}\right) \left(\sin \frac{4\pi}{5}\right)$$

$$+ \left(\frac{\pi}{5}\right) \left(\sin \frac{5\pi}{5}\right)$$

$$\sum_{Q=1}^5 \left(\frac{\pi}{5}\right) \left(\sin \frac{Q\pi}{5}\right)$$

$$\text{sum}(\text{seq}\left(\left(\frac{\pi}{5}\right) \left(\sin \frac{x\pi}{5}\right), x, 1, 5\right))$$

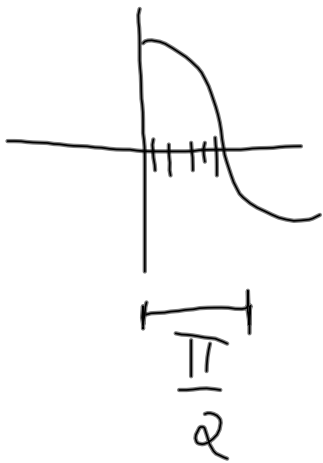
add up all the terms in the sequence. what seq?

create a sequence based on this pattern

where this changes

starting with 1 and going up by 1 until I'm done

④  $\cos(x)$   $[0, \pi/2]$



$2 = n$

$$\left(\frac{\pi}{4}\right)\left(\cos\left(\frac{\pi}{4}\right)\right) + \left(\frac{\pi}{4}\right)\left(\cos\left(\frac{2\pi}{4}\right)\right)$$

$5 = n$

$$\left(\frac{\pi}{10}\right)\left(\cos\left(\frac{\pi}{10}\right)\right) + \left(\frac{\pi}{10}\right)\left(\cos\left(\frac{2\pi}{10}\right)\right) + \left(\frac{\pi}{10}\right)\left(\cos\left(\frac{3\pi}{10}\right)\right) + \left(\frac{\pi}{10}\right)\left(\cos\left(\frac{4\pi}{10}\right)\right) + \left(\frac{\pi}{10}\right)\left(\cos\left(\frac{5\pi}{10}\right)\right)$$

$10 = n$

$$\left(\frac{\pi}{20}\right)\left(\cos\left(\frac{\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{2\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{3\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{4\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{5\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{6\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{7\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{8\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{9\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{10\pi}{20}\right)\right)$$

$$\left(\frac{\pi}{20}\right)\left(\cos\left(\frac{\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{2\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{3\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{4\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{5\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{6\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{7\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{8\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{9\pi}{20}\right)\right) + \left(\frac{\pi}{20}\right)\left(\cos\left(\frac{10\pi}{20}\right)\right)$$

9/94